



Polarimetric Multi-View Inverse Rendering (Polarimetric MVIR)

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Introduction

Polarization Camera

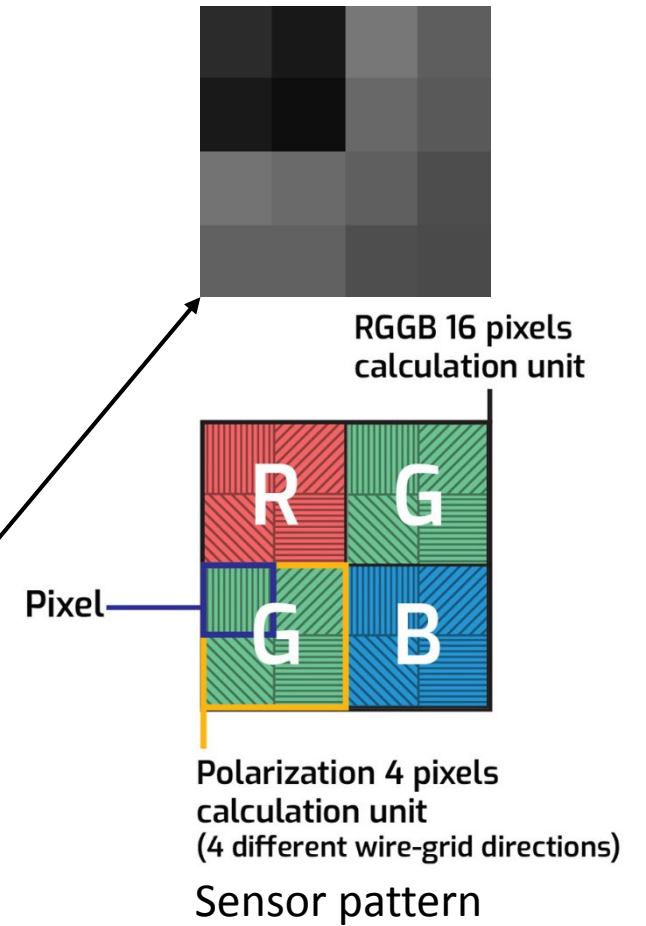
Scene



One-shot polarization camera
(Lucid PHX050S-Q camera)



Captured mosaic raw data



Polarization Data Acquisition



Raw data

| | | | |
|-----|----|-----|----|
| 90 | 45 | 90 | 45 |
| 135 | 0 | 135 | 0 |
| 90 | 45 | 90 | 45 |
| 135 | 0 | 135 | 0 |

Sensor pattern



Polarizer's direction

Demosaicking

0

45

90

135

I_0

I_{45}

I_{90}

I_{135}

Polarization images

Polarization Data Acquisition

Stokes vector

$$\mathbf{s} = \begin{bmatrix} S_0 \\ S_1 \\ S_2 \\ S_3 \end{bmatrix} = \begin{bmatrix} I_{max} + I_{min} \\ (I_{max} - I_{min})\cos(2\phi) \\ (I_{max} - I_{min})\sin(2\phi) \\ 0 \end{bmatrix} = \begin{bmatrix} I_0 + I_{90} \\ I_0 - I_{90} \\ I_{45} - I_{135} \\ 0 \end{bmatrix}$$

➤ Intensity information

$$I = s_0$$

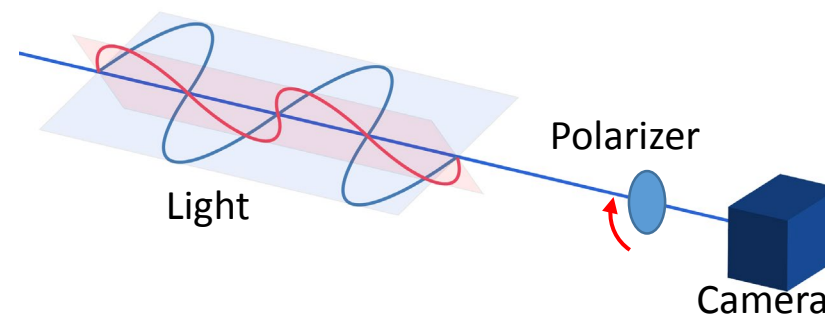
➤ Polarimetric information

- Angle of Polarization (AoP)

$$\phi = \frac{1}{2} \tan^{-1} \frac{s_2}{s_1}$$

- Degree of Polarization (DoP)

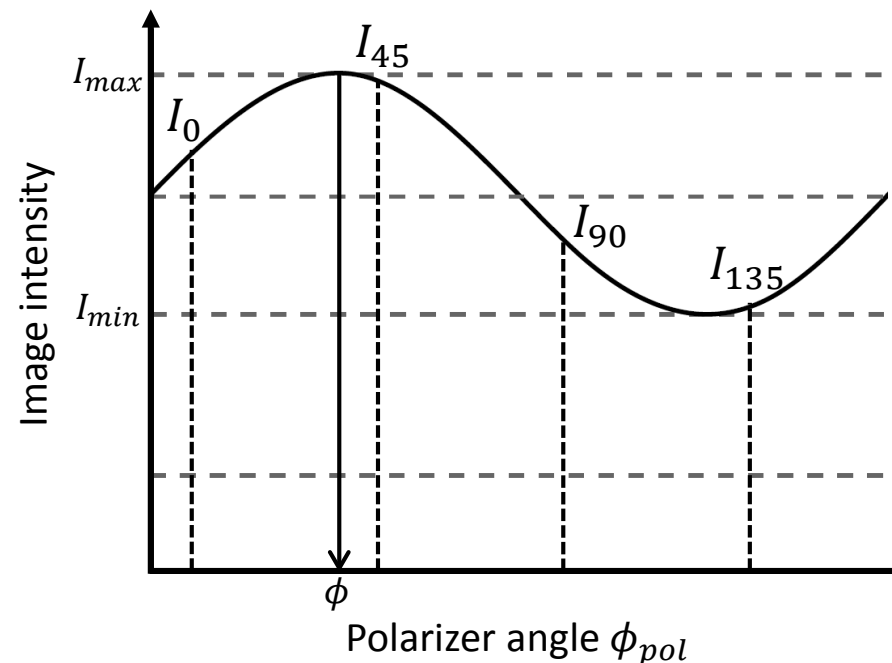
$$\rho = \frac{\sqrt{s_1^2 + s_2^2}}{s_0}$$



$$I(\phi_{pol}) = \frac{I_{max} + I_{min}}{2} + \frac{I_{max} - I_{min}}{2} \cos(2(\phi_{pol} - \phi))$$

ϕ : Angle of polarization

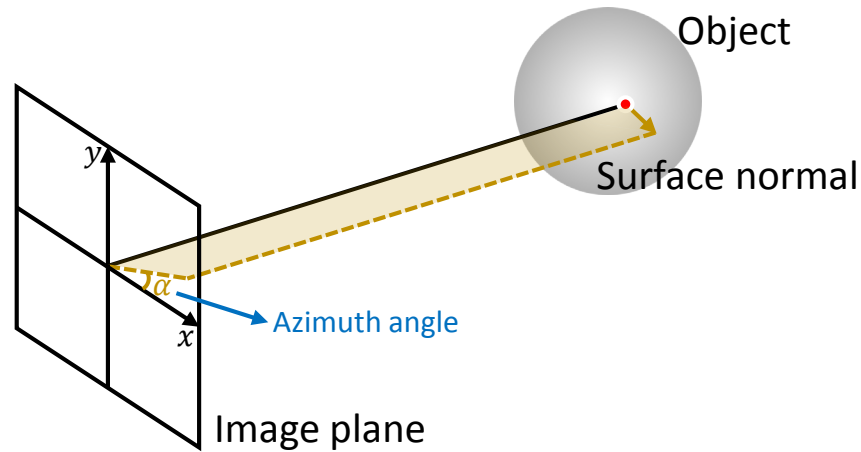
ϕ_{pol} : Polarizer angle of the sensor



Relationship Between AoP and Surface Normal

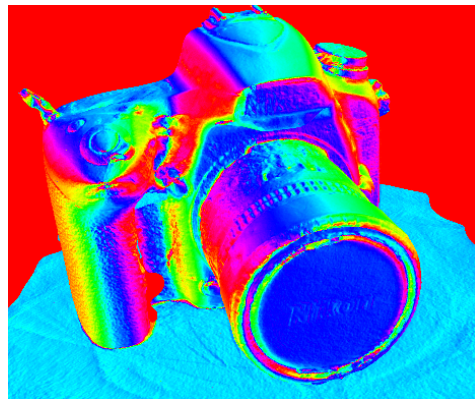
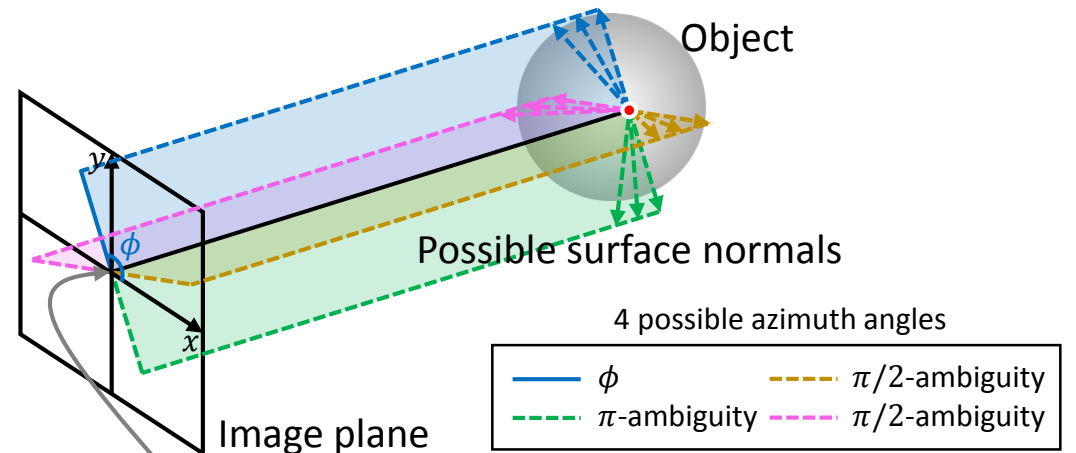
- Azimuth angle (α)**

The angle between x -axis and projection of the surface normal to the image plane.



- AoP (ϕ) and possible azimuth angles**

Polarized specular reflection dominates: $|\phi - \alpha| = \pi/2$
 Polarized diffuse reflection dominates: $|\phi - \alpha| = 0$ or π



Azimuth angle map

Related with ambiguities

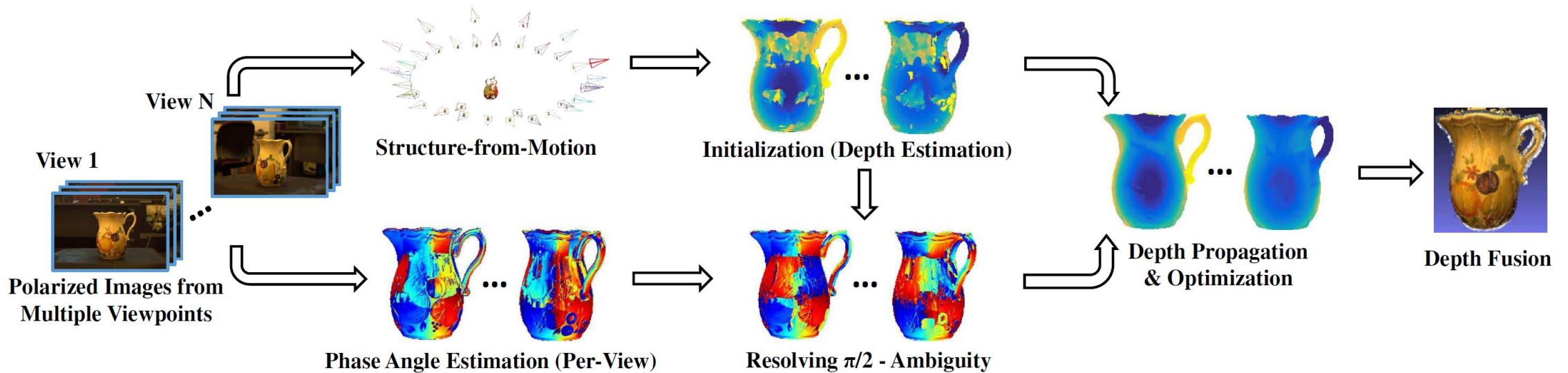


AoP image

Related Work: Polarimetric Multi-View Stereo

➤ **State-of-the-art multi-view stereo method using polarization camera**

- Calculate AoP and resolve ambiguities
- Propagate the depth according to disambiguated AoP
- Optimize and fuse the depth

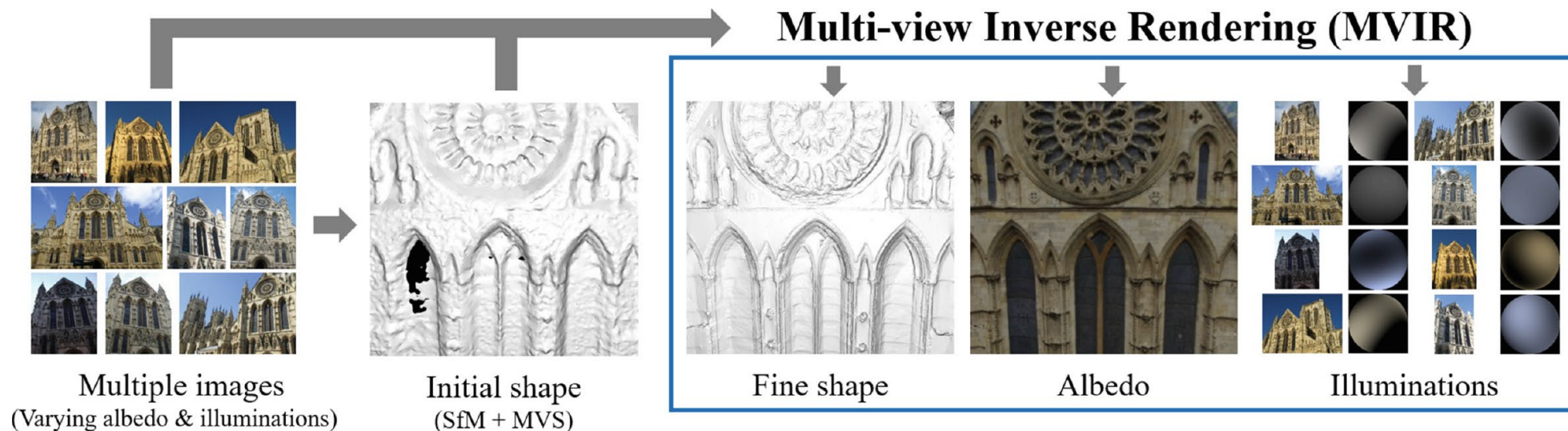


Cui, Z., Gu, J., Shi, B., Tan, P., Kautz, J.: Polarimetric multi-view stereo. (CVPR 2017)

Related Work: Multi-View Inverse Rendering

➤ **State-of-the-art method combining photometry and geometry**

- Input RGB images, camera poses and initial 3D shape
- Solve an optimization problem using photometric and geometric information
- Derive detailed shape, albedo and illumination



Kim, K., Torii, A., Okutomi, M.: Multi-view inverse rendering under arbitrary illumination and albedo. (ECCV 2016)

Our Contributions

We propose Polarimetric MVIR:

- The first method based on multi-view photometric and polarimetric optimization with an inverse rendering framework.

| Method | Geometry | Photometry | Polarimetry |
|--------------------------|----------|------------|-------------|
| Polarimetric MVS | ✓ | | ✓ |
| MVIR | ✓ | ✓ | |
| Polarimetric MVIR (Ours) | ✓ | ✓ | ✓ |

- A novel polarimetric cost function is proposed to effectively constrain the surface normal while considering ambiguities as an optimization problem.



Proposed Method

Polarimetric MVIR: Input Data

Scene



Raw image

Polarimetric MVIR: Input Data

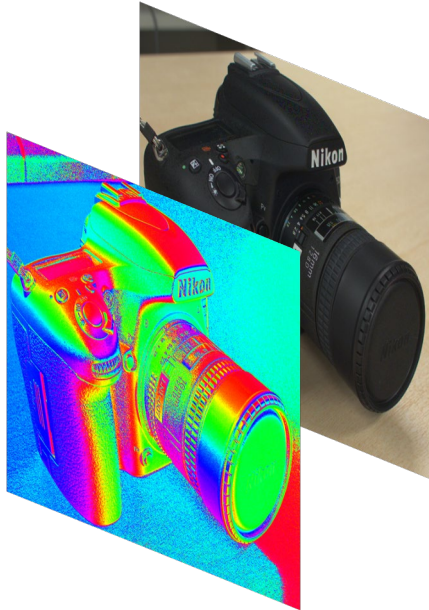
Scene



I_{min} and ϕ 's calculation

$$\mathbf{s} = \begin{bmatrix} s_0 \\ s_1 \\ s_2 \end{bmatrix} = \begin{bmatrix} I_0 + I_{90} \\ I_0 - I_{90} \\ I_{45} - I_{135} \end{bmatrix}$$

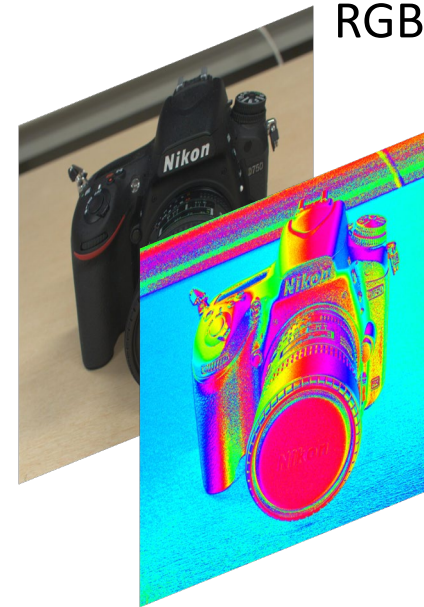
$$\begin{cases} I_{min} = \frac{s_0 - \sqrt{s_1^2 + s_2^2}}{2} \\ \phi = \frac{1}{2} \tan^{-1} \frac{s_2}{s_1} \end{cases}$$



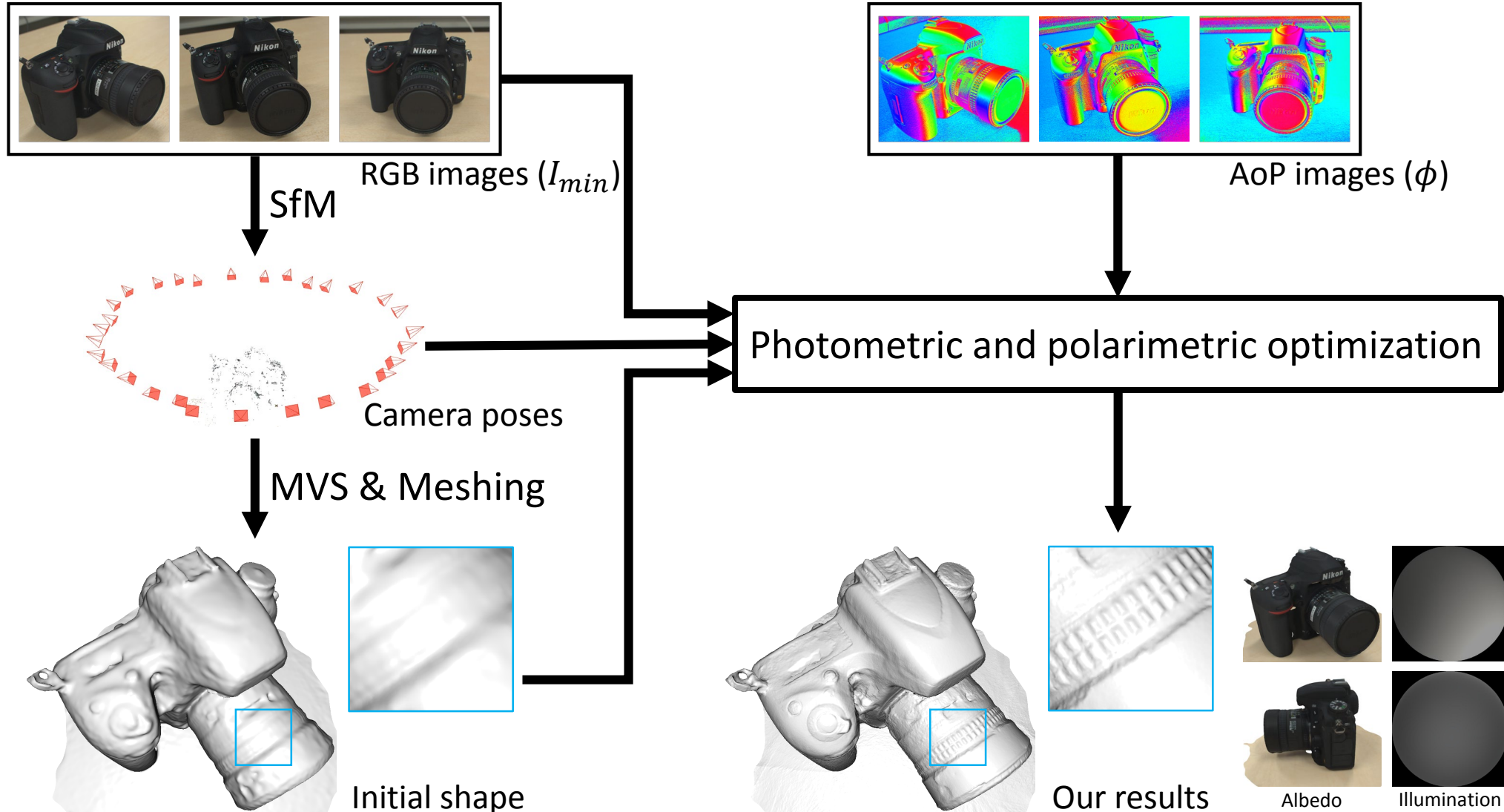
RGB image (I_{min})



AoP image (ϕ)



Polarimetric MVIR: Overview

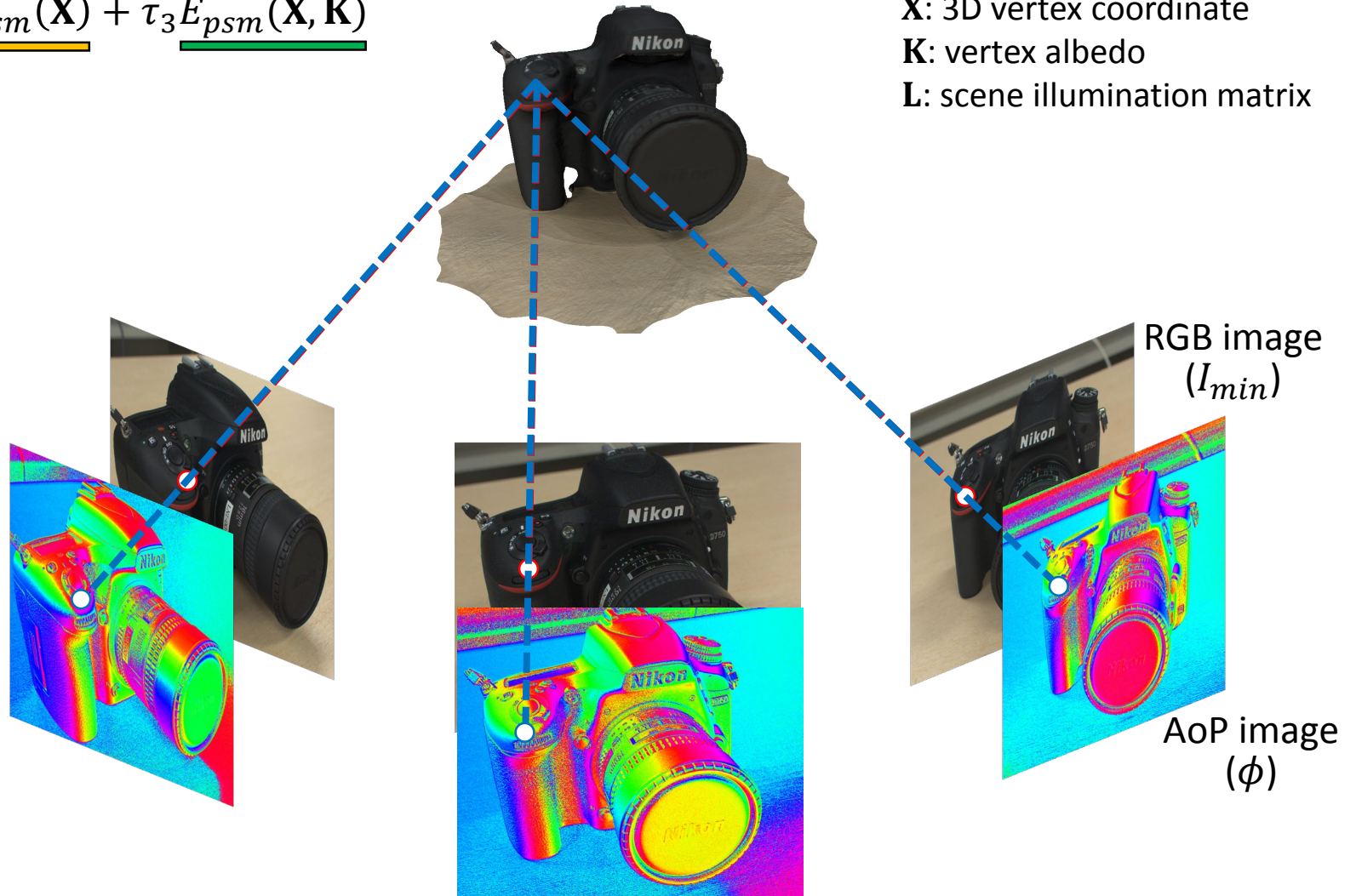


Multi-View Photometric and Polarimetric Optimization

$$\arg \min_{\mathbf{X}, \mathbf{K}, \mathbf{L}} \underbrace{E_{pho}(\mathbf{X}, \mathbf{K}, \mathbf{L})}_{\text{red}} + \tau_1 \underbrace{E_{pol}(\mathbf{X})}_{\text{blue}} + \tau_2 \underbrace{E_{gsm}(\mathbf{X})}_{\text{yellow}} + \tau_3 \underbrace{E_{psm}(\mathbf{X}, \mathbf{K})}_{\text{green}}$$

- Photometric error term
- Polarimetric error term
- Geometric smoothness term
- Photometric smoothness term

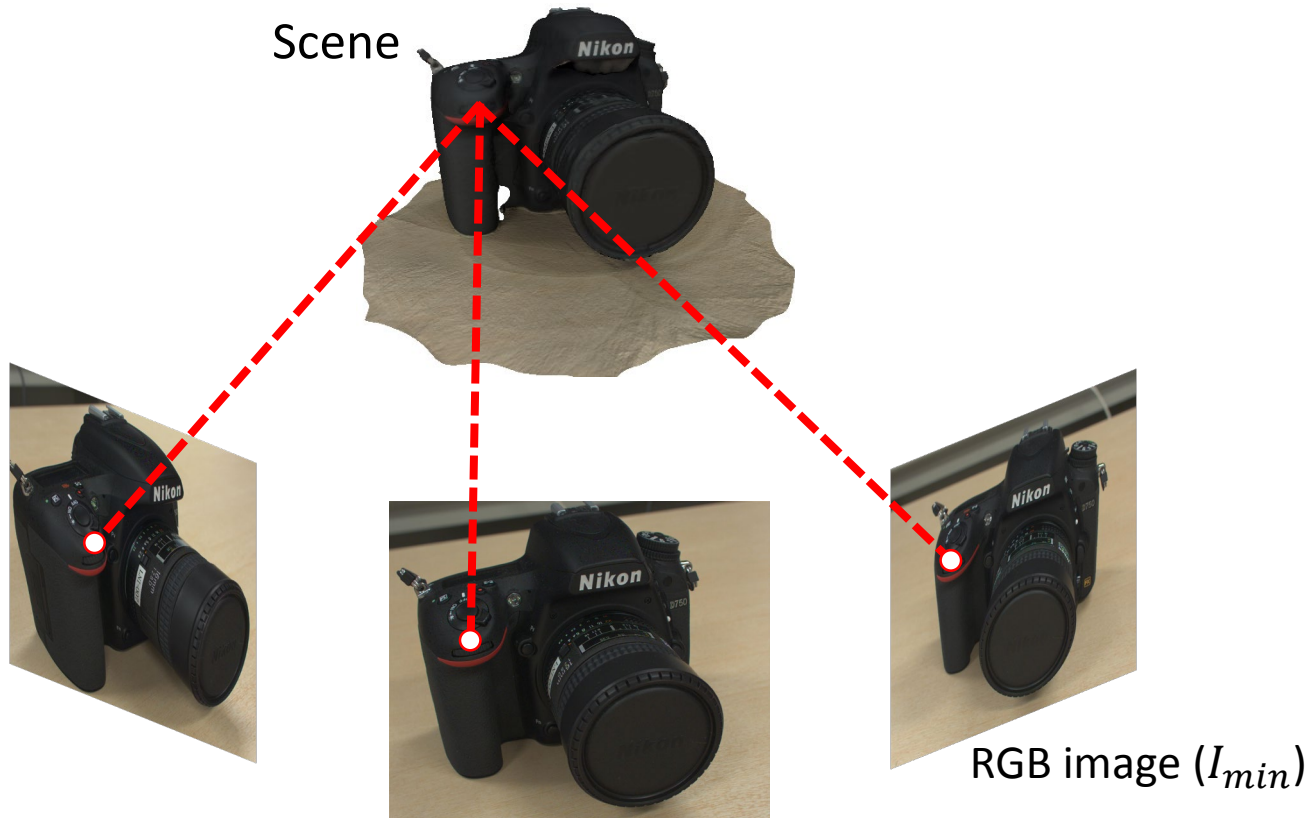
\mathbf{X} : 3D vertex coordinate
 \mathbf{K} : vertex albedo
 \mathbf{L} : scene illumination matrix



Multi-View Photometric and Polarimetric Optimization

$$\arg \min_{\mathbf{X}, \mathbf{K}, \mathbf{L}} \underline{E_{pho}(\mathbf{X}, \mathbf{K}, \mathbf{L})} + \tau_1 E_{pol}(\mathbf{X}) + \tau_2 E_{gsm}(\mathbf{X}) + \tau_3 E_{psm}(\mathbf{X}, \mathbf{K})$$

- Photometric error term



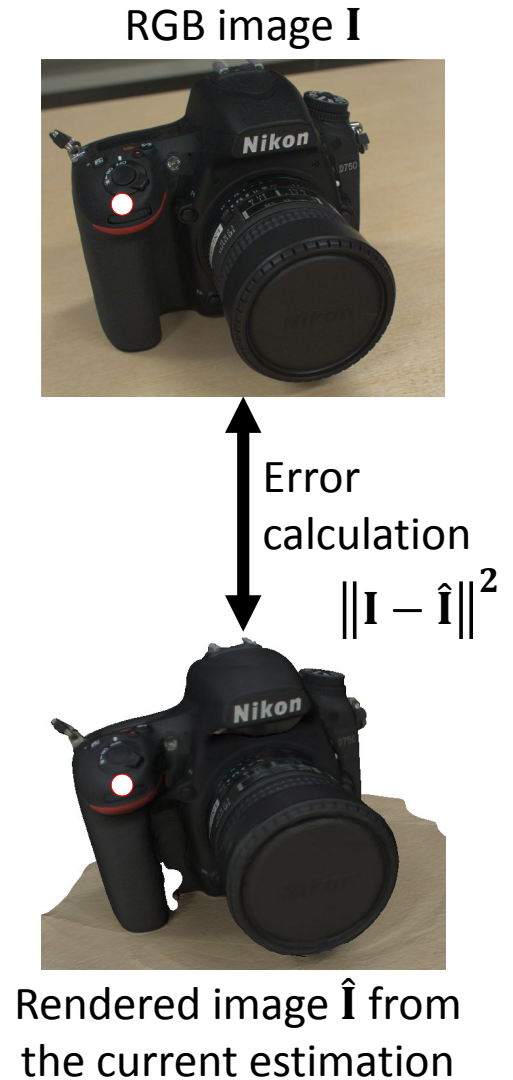
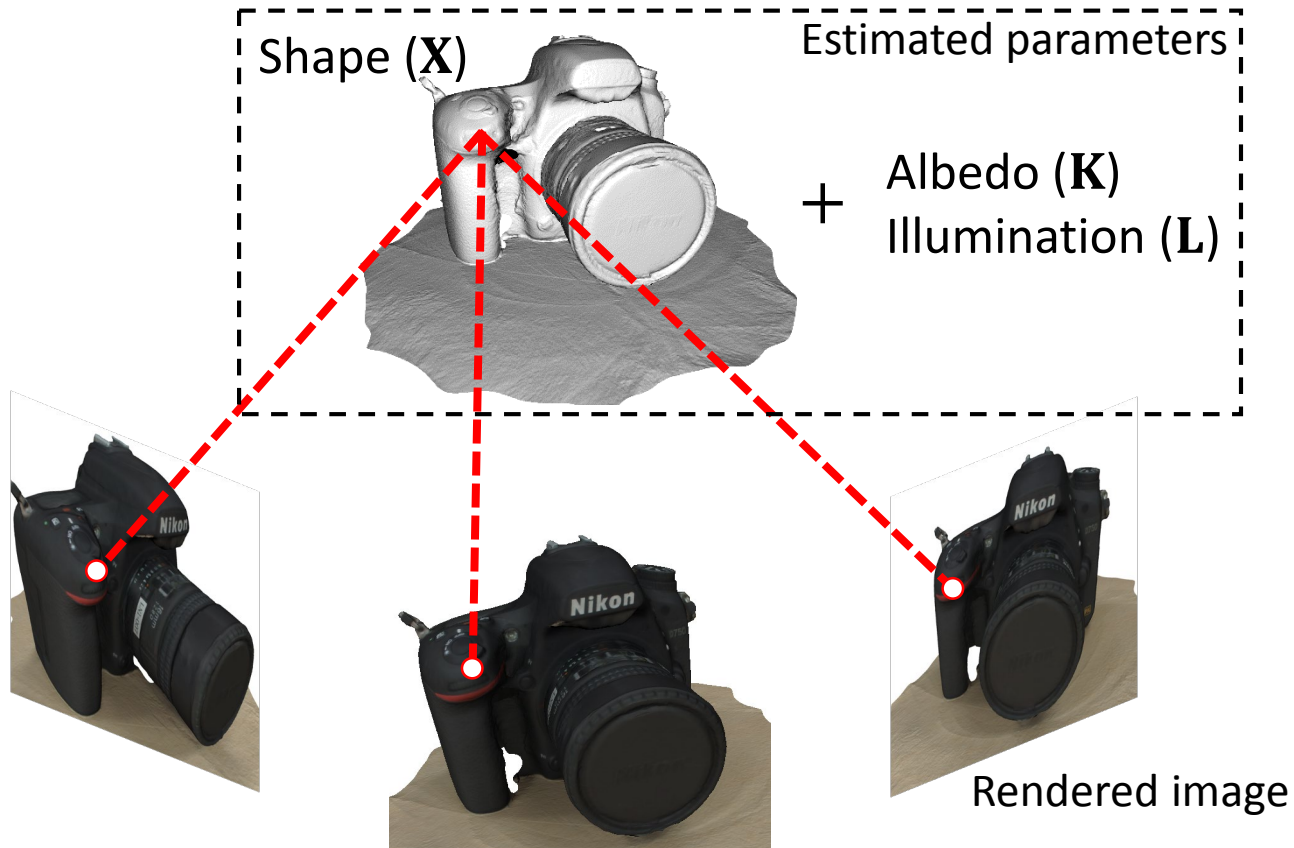
RGB image I



Multi-View Photometric and Polarimetric Optimization

$$\arg \min_{\mathbf{X}, \mathbf{K}, \mathbf{L}} \underline{E_{pho}(\mathbf{X}, \mathbf{K}, \mathbf{L})} + \tau_1 E_{pol}(\mathbf{X}) + \tau_2 E_{gsm}(\mathbf{X}) + \tau_3 E_{psm}(\mathbf{X}, \mathbf{K})$$

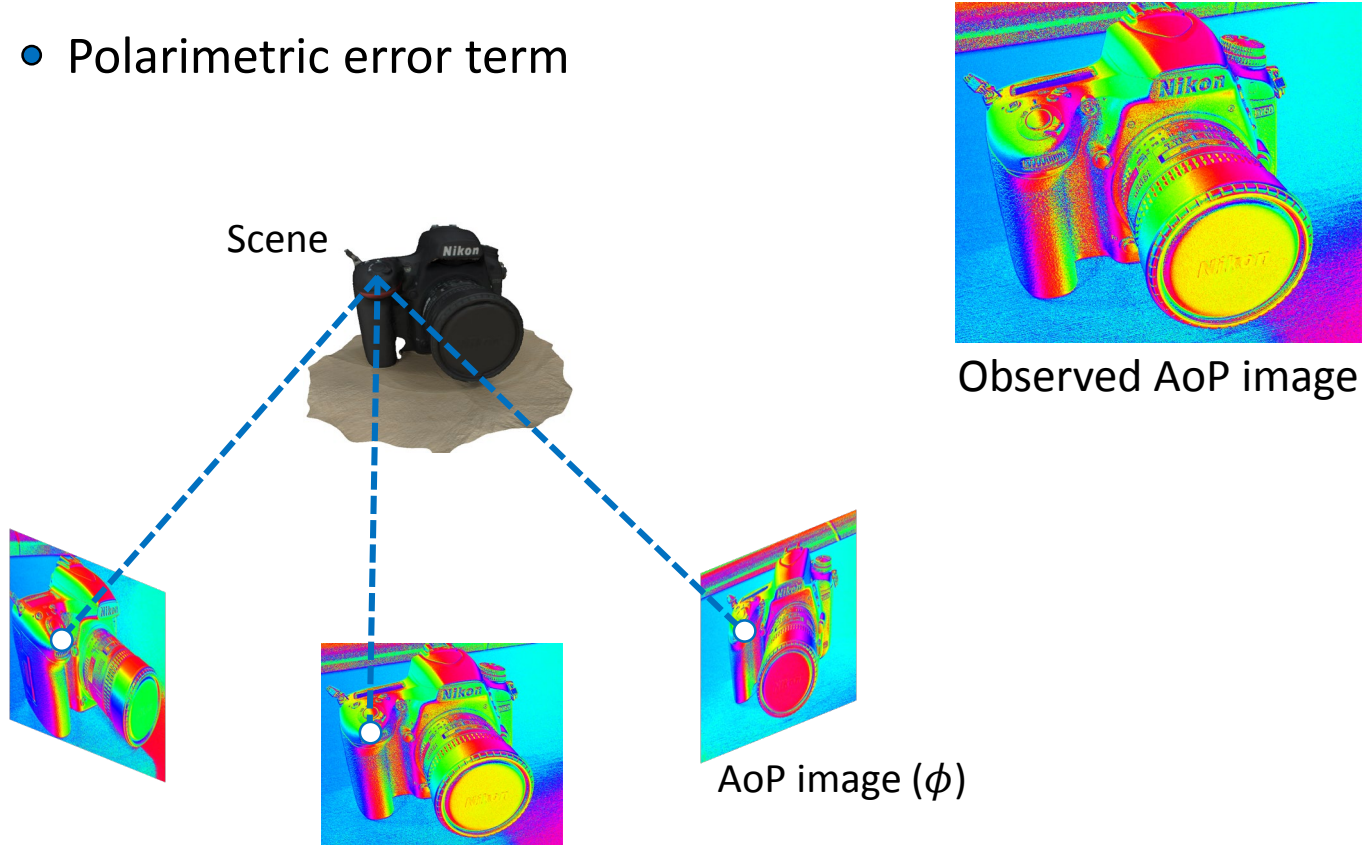
- Photometric error term



Multi-View Photometric and Polarimetric Optimization

$$\arg \min_{\mathbf{X}, \mathbf{K}, \mathbf{L}} E_{pho}(\mathbf{X}, \mathbf{K}, \mathbf{L}) + \tau_1 \underline{E_{pol}(\mathbf{X})} + \tau_2 E_{gsm}(\mathbf{X}) + \tau_3 E_{psm}(\mathbf{X}, \mathbf{K})$$

- Polarimetric error term

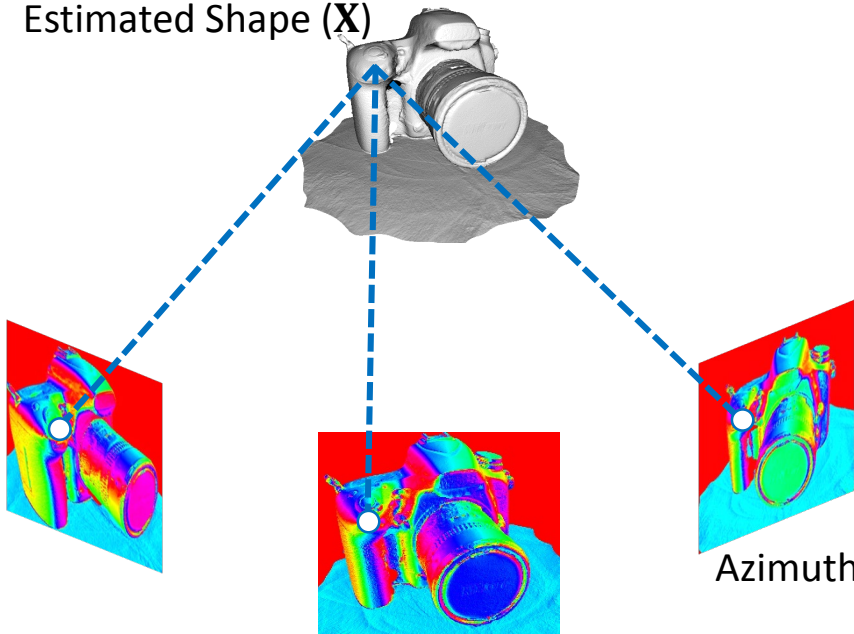


Multi-View Photometric and Polarimetric Optimization

$$\arg \min_{\mathbf{X}, \mathbf{K}, \mathbf{L}} E_{pho}(\mathbf{X}, \mathbf{K}, \mathbf{L}) + \tau_1 E_{pol}(\mathbf{X}) + \tau_2 E_{gsm}(\mathbf{X}) + \tau_3 E_{psm}(\mathbf{X}, \mathbf{K})$$

- Polarimetric error term

Estimated Shape (\mathbf{X})



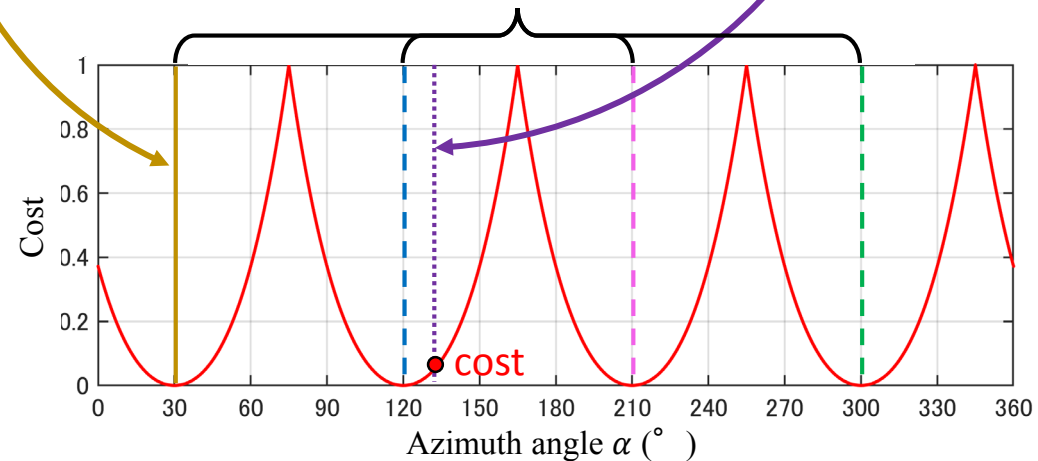
Observed AoP image

Error calculation
considering ambiguities



Azimuth angle from
the current estimation

Four possible azimuth angles



Our proposed cost function ($\phi = 30^\circ$)

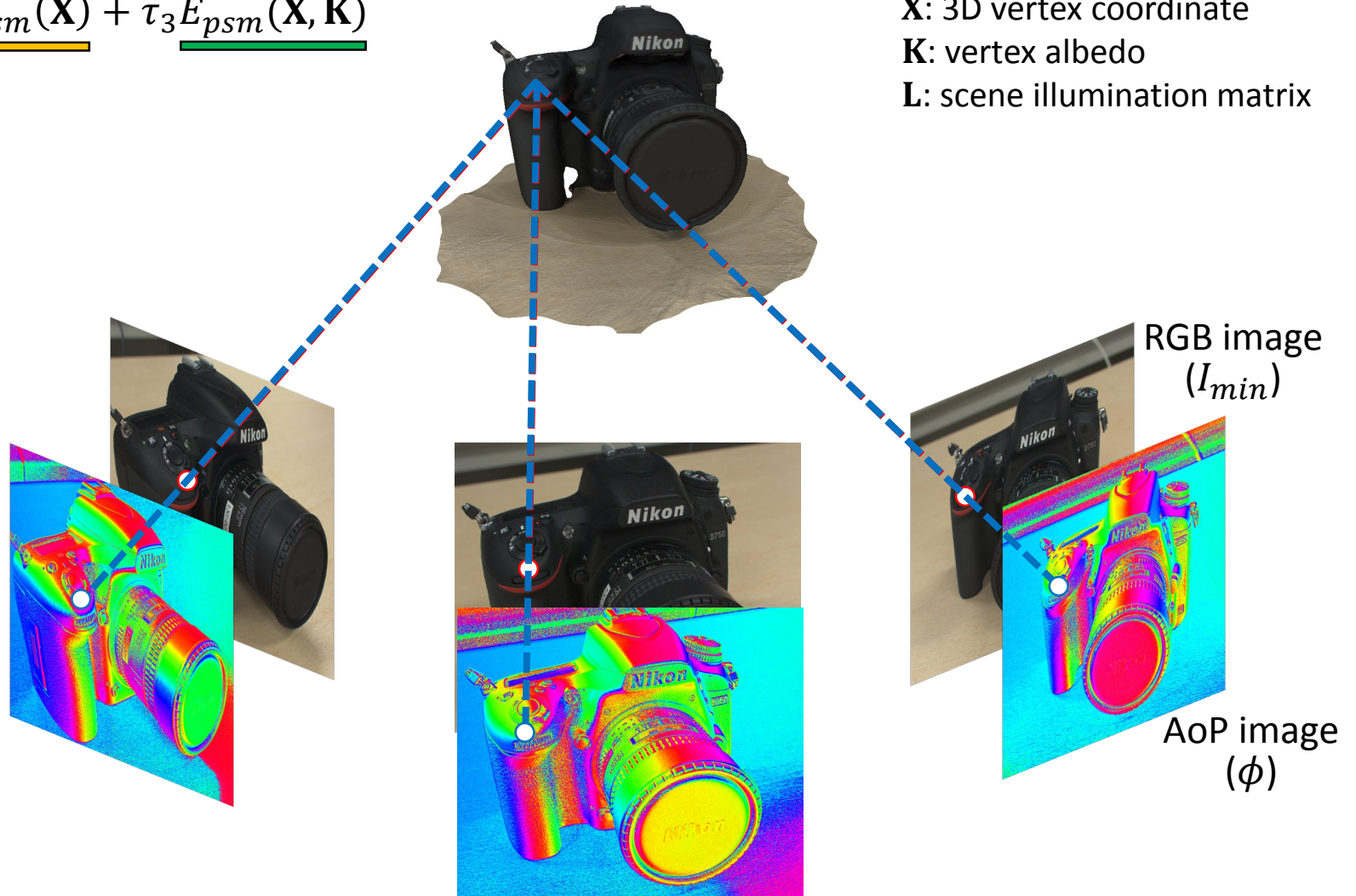
Multi-View Photometric and Polarimetric Optimization

$$\arg \min_{\mathbf{X}, \mathbf{K}, \mathbf{L}} \underbrace{E_{pho}(\mathbf{X}, \mathbf{K}, \mathbf{L})}_{\text{red}} + \underbrace{\tau_1 E_{pol}(\mathbf{X})}_{\text{blue}} + \underbrace{\tau_2 E_{gsm}(\mathbf{X})}_{\text{yellow}} + \underbrace{\tau_3 E_{psm}(\mathbf{X}, \mathbf{K})}_{\text{green}}$$

- Photometric error term
- Polarimetric error term
- Geometric smoothness term
- Photometric smoothness term

Equations and more details can be seen in our paper.

\mathbf{X} : 3D vertex coordinate
 \mathbf{K} : vertex albedo
 \mathbf{L} : scene illumination matrix





Real Scene Results

Camera (31 views) - Our Results



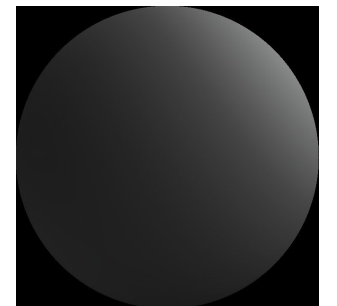
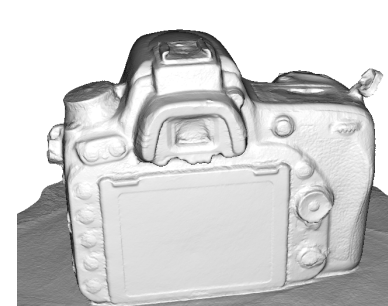
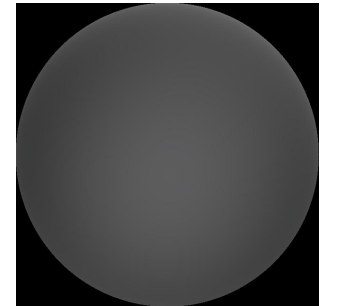
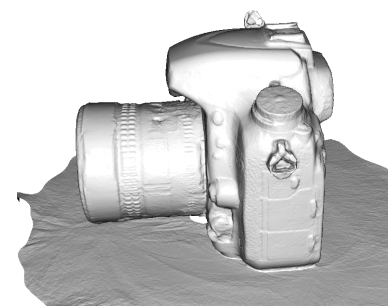
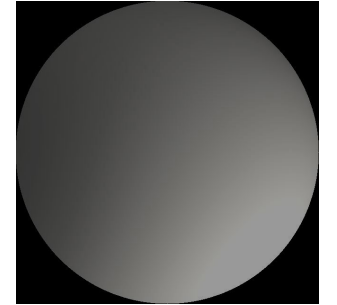
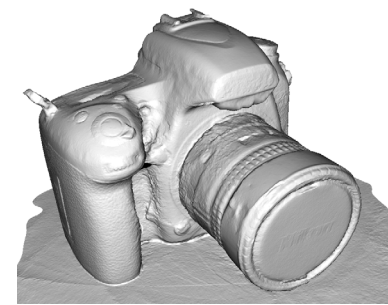
RGB images



AoP images



Estimated camera poses



Input image

Estimated albedo

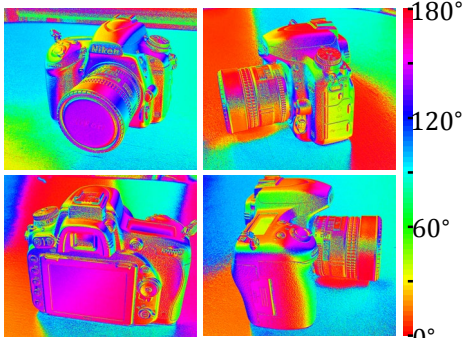
Estimated shape

Estimated illumination

Camera (31 views) - Comparison



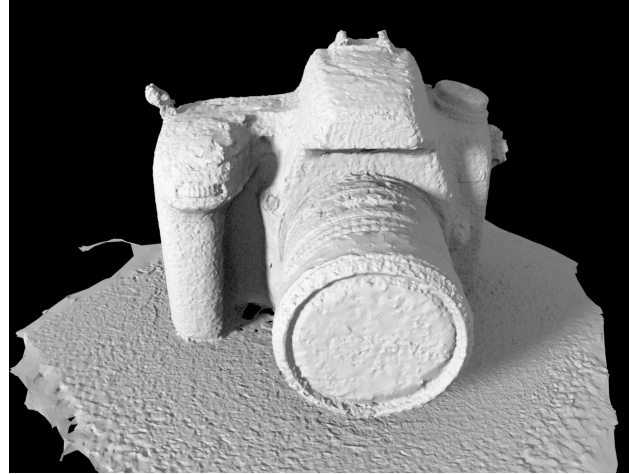
RGB images



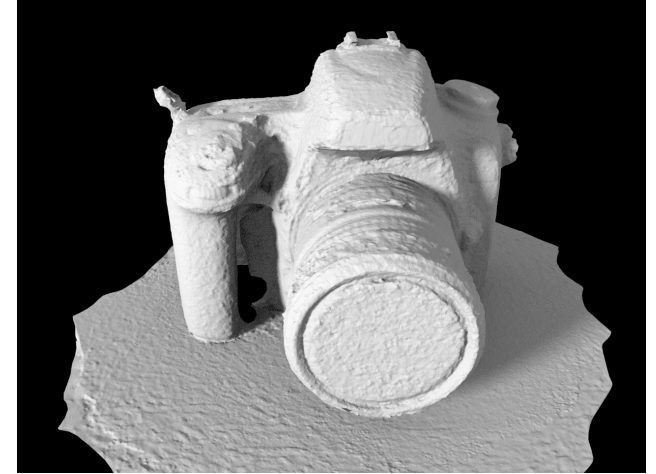
AoP images



Estimated camera poses



CPMVS



OpenMVS



MVIR

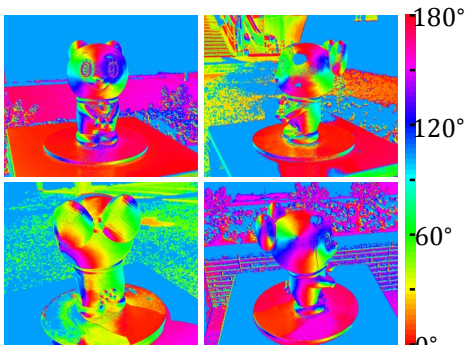
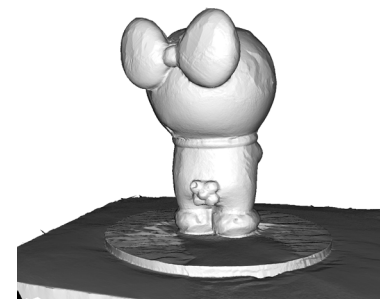
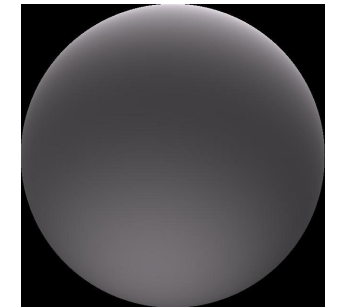
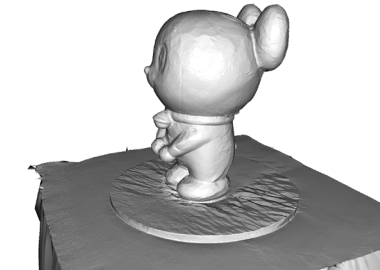
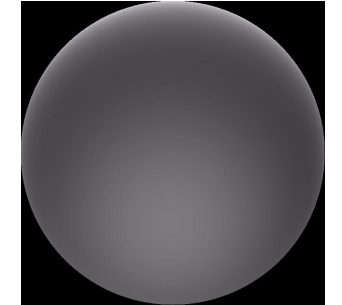
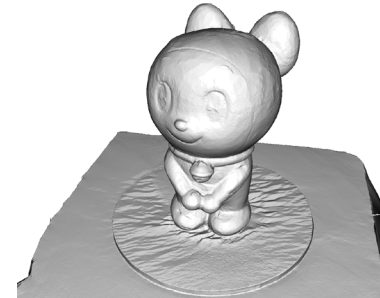


Polarimetric MVIR (Ours)

Statue (43 views) - Our Results



RGB images



AoP images



Estimated camera poses

Input image

Estimated albedo

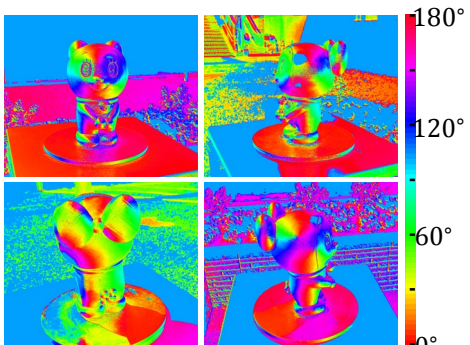
Estimated shape

Estimated illumination

Statue (43 views) - Comparison



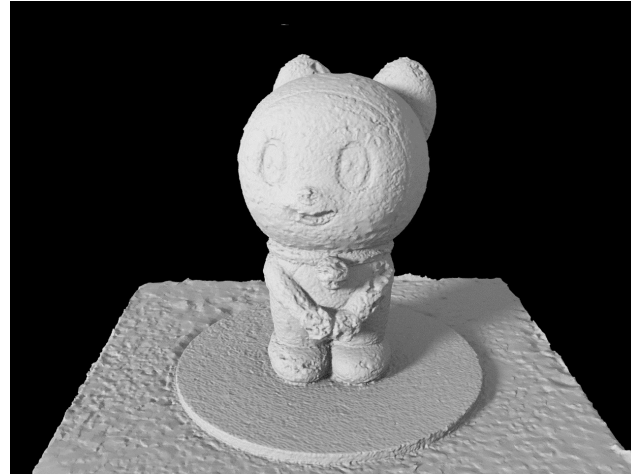
RGB images



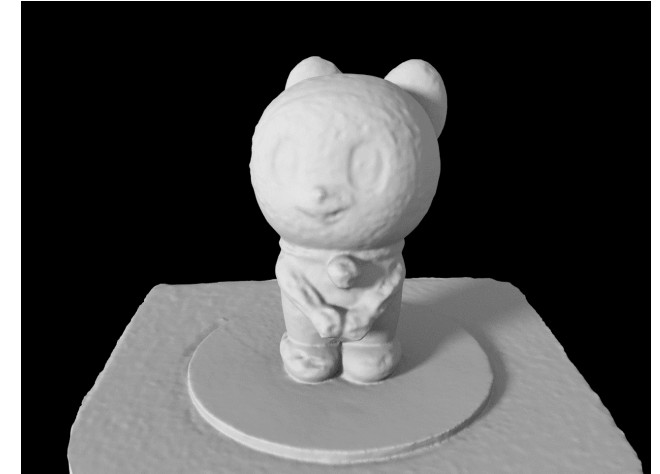
AoP images



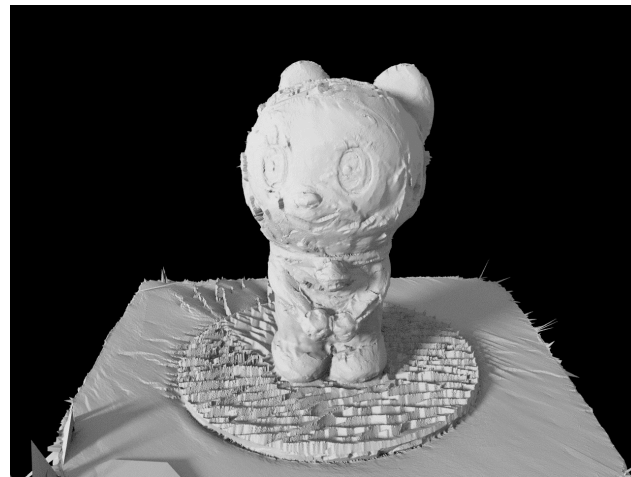
Estimated camera poses



CMPMVS



OpenMVS



MVIR

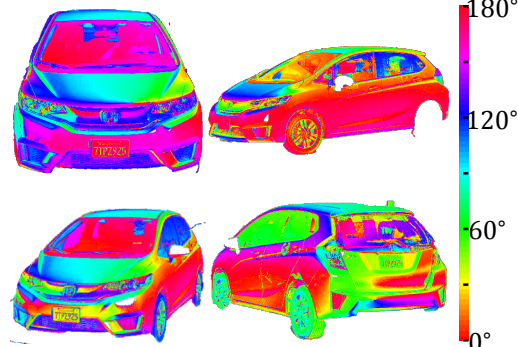


Polarimetric MVIR (Ours)

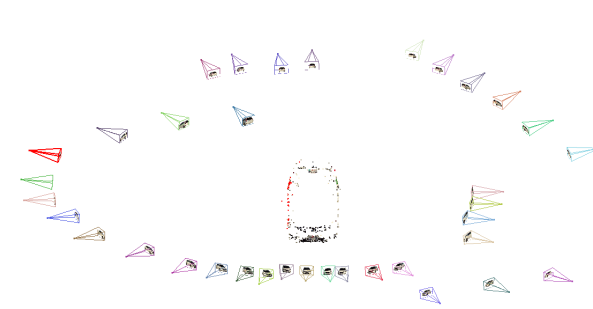
Refinement for Polarimetric MVS: Car (36 views)



RGB images



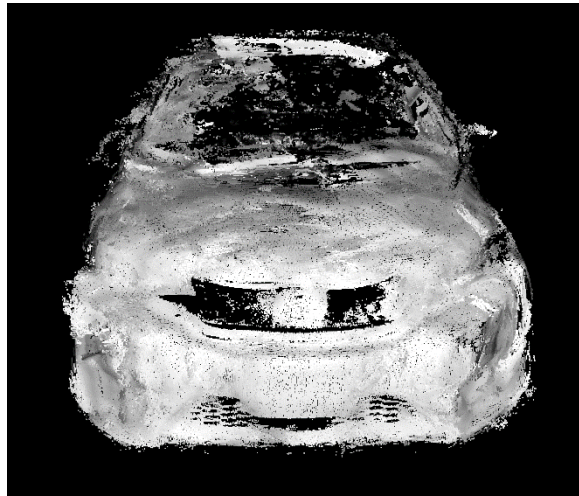
AoP images



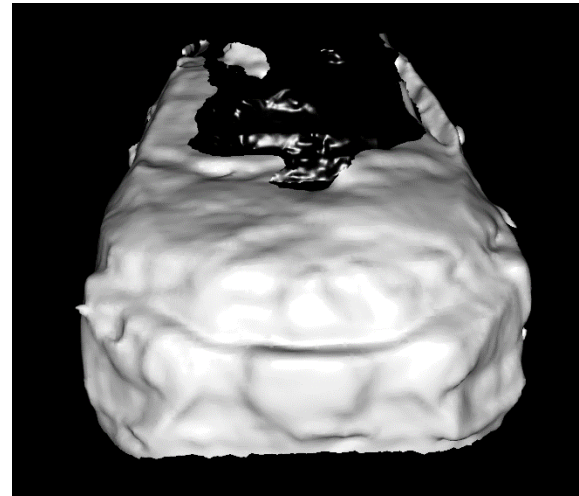
Estimated camera poses



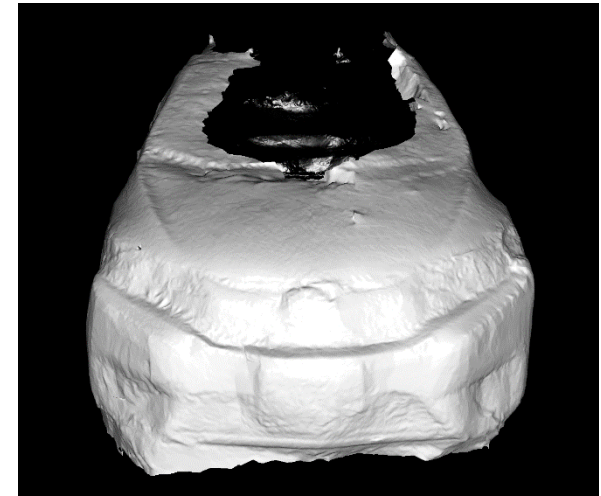
MVS (Gipuma)
without polarization



Polarimetric MVS



Polarimetric MVS + Poisson

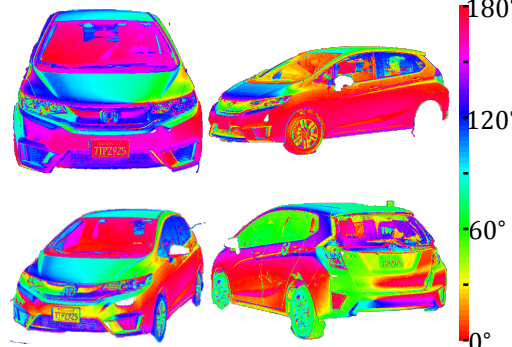


Polarimetric MVIR (Ours)

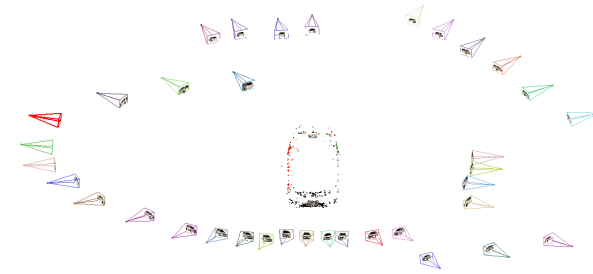
Refinement for Polarimetric MVS: Car (36 views)



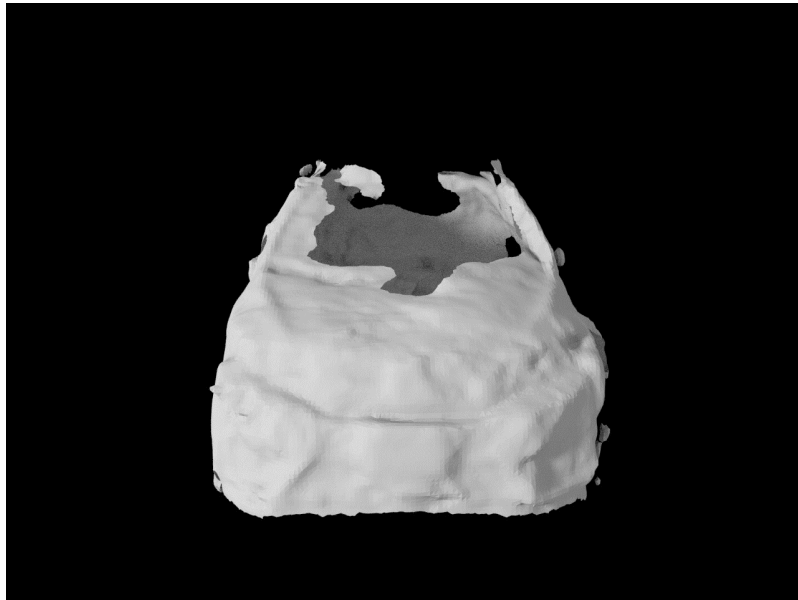
RGB images



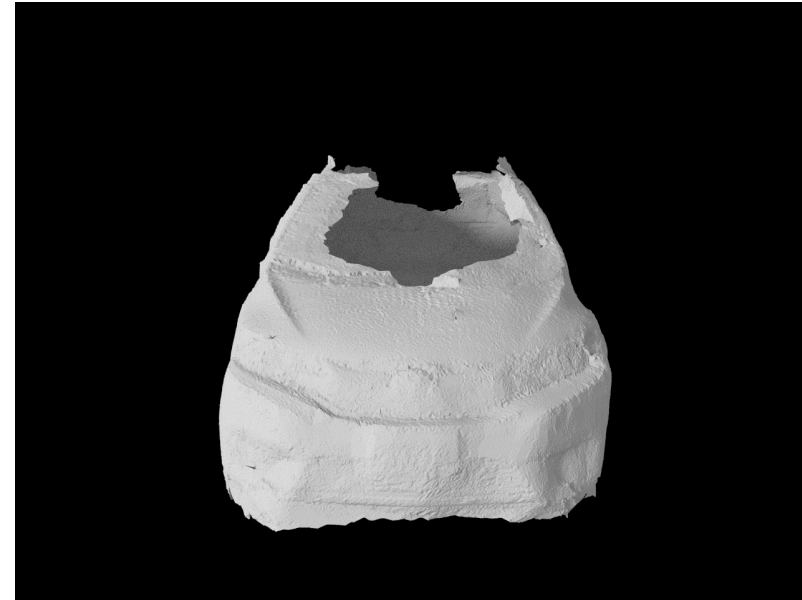
AoP images



Estimated camera poses



Polarimetric MVS + Poisson



Polarimetric MVIR (Ours)

Conclusions

We have proposed Polarimetric MVIR:

- Use a one-shot polarization camera to capture the data and perform SfM and MVS. Data and results are input to a photometric and polarimetric optimization problem.
- Reconstruct high-quality 3D models by optimizing multi-view photometric rendering errors and polarimetric errors.
- Resolve ambiguities implicitly as an optimization problem, making the proposed method fully passive and applicable to various materials under different situations.
- Robust to ambiguities and noise, and can generate more detailed 3D models compared with existing state-of-the-art multi-view reconstruction methods.



THANK YOU FOR LISTENING